

Interface Flux Recovery Method for Ocean-Atmosphere Coupling

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- **Objective:**

- Develop efficient, accurate, and stable coupling schemes for Earth system models that allow for partitioned solves of each component, but retain stability properties of an underlying monolithic problem.

- **Approach:**

- Start with a well-posed monolithic mixed-like formulation
- Use a Schur complement to isolate and obtain an accurate estimate of the flux across the interface between the models
- Decouple the individual components resulting in a non-iterative partitioned scheme with special treatment of the flux

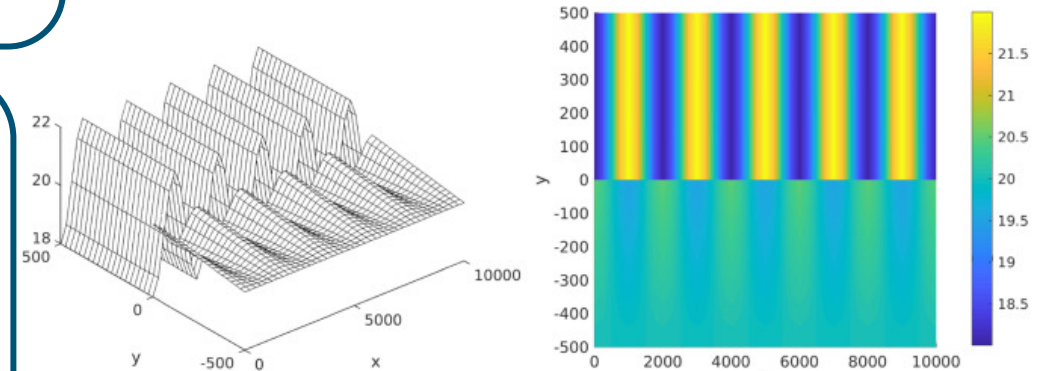
- **Impact:**

- Derived IFR method for coupling a simple heat transfer model in the ocean-atmosphere with a bulk condition at the interface
- Demonstrated on a simplified test case with an exact solution for the bulk condition system
- Achieved expected convergence rates for matching and non-matching grids

The diagram illustrates the interface between the atmosphere (top) and the ocean (bottom). The interface is labeled with the Greek letter Γ . The governing equations for simplified atmosphere/ocean heat transfer are:

$$\dot{T}_a + \frac{\partial}{\partial x}(u_a T_a) = \frac{\partial}{\partial z} K_a \frac{\partial T_a}{\partial z}$$
$$K_a \frac{\partial T_a}{\partial z} = K_o \frac{\partial T_o}{\partial z} = \alpha(T_a - T_o)$$
$$\dot{T}_o + \frac{\partial}{\partial x}(u_o T_o) = \frac{\partial}{\partial z} K_o \frac{\partial T_o}{\partial z}$$

Governing equations for simplified atmosphere/ocean heat transfer



Test case combining a wave in the horizontal direction with a discontinuity driving the bulk condition at the interface

K. Chad Sockwell, Kara Peterson, Paul Kuberry, Pavel Bochev, Nat Trask, (2020) Interface Flux Recovery coupling method for the ocean-atmosphere system, *Results in Applied Mathematics*, 8, <https://doi.org/10.1016/j.rinam.2020.100110>.